

Penn WSJ Non-Terminals (NTs)

- Basic non-terminal tagset (not including pre-terminals)

ADJP	Adjective Phrase	ADVP	Adverbial Phrase	CONJP	Conjunction Phrase
FRAG	Fragment	INTJ	Interjection	LST	List marker
NAC	Not a Constituent	NP	Noun Phrase	NX	Complex NP
PP	Prepositional Phrase	PRN	Parenthetical	PRT	Particle
QP	Quantifier Phrase	RRC	Reduced Relative Clause	S	Simple Clause
SBAR	Subordinate Clause	SBARQ	Subordinate Question Clause	SINV	Inverted Clause
SQ	Inverted Question	UCP	Unlike Coordinated Phrase	VP	Verb Phrase
WHADJP	Wh-adjective Phrase	WHAVP	Wh-adverb Phrase	WHNP	Wh-noun Phrase
WHPP	Wh-prepositional Phrase	X	Unknown		

- Other “function” tags may label constituents, e.g. PP-TMP means temporal PP
- Raw treebank contains empty categories

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7

Why treebanks?

- Treebanks are critical to training statistical parsers
- Also valuable to linguist when investigating phenomena

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8

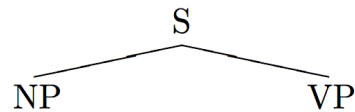
Grammar Induction

- Extract context-free rules from trees in the treebank
- Context-free rules of the form:
 $A \rightarrow B C D E$
 - where A is the (one and only) ‘parent’
 - and B, C, D, and E are the ‘children’
 - also refer to left-hand side (LHS): A and right-hand side (RHS): B C D E

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9

CFG Induction



- Local tree: Parent (S), children (NP VP)
- Each local tree represents a context-free rule:
 $S \rightarrow NP VP$

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10

Interpretations of a CFG rule

- For a rule such as $S \rightarrow NP VP$, there are various interpretations of what this means
- Derivations:
 - An NP and a VP can combine (or compose) to produce an S
 - An S can be split into an NP followed by a VP
- Trees:
 - An S node can generate an NP and a VP node
 - An S node can be the parent of an NP and a VP node

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11

Derivations

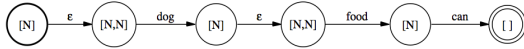
- If we have a rule $A \rightarrow \alpha$, then define a *derives* relation: $\beta A \gamma \Rightarrow \beta \alpha \gamma$.
- A string $w_1 \dots w_n$ is in the language of a CFG G if $S \vdash \Rightarrow^* w_1 \dots w_n$
- For example, consider these noun compounding rules:
 (i) $N \rightarrow N N$ (ii) $N \rightarrow \text{dog}$ (iii) $N \rightarrow \text{food}$ (iv) $N \rightarrow \text{can}$
- There are many possible derivations, s.t. $N \Rightarrow^* \text{dog food can}$
 1. $N \Rightarrow N N \Rightarrow N \text{can} \Rightarrow N N \text{can} \Rightarrow N \text{food can} \Rightarrow \text{dog food can}$
 2. $N \Rightarrow N N \Rightarrow N N N \Rightarrow N N \text{can} \Rightarrow N \text{food can} \Rightarrow \text{dog food can}$
 3. $N \Rightarrow N N \Rightarrow N N N \Rightarrow \text{dog} N N \Rightarrow \text{dog food} N \Rightarrow \text{dog food can}$
 4. $N \Rightarrow N N \Rightarrow \text{dog} N \Rightarrow \text{dog} N N \Rightarrow \text{dog food} N \Rightarrow \text{dog food can}$
 5. ...
- Derivation 1. is the *rightmost* derivation, always expanding the rightmost non-terminal; derivation 4. is a *leftmost* derivation

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12

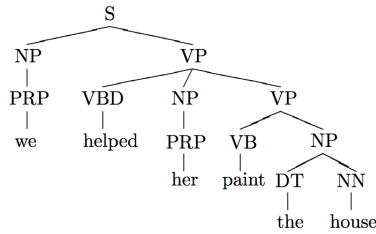
Pushdown automata

- Consider the leftmost derivation:
 $N \Rightarrow N N \Rightarrow \text{dog } N \Rightarrow \text{dog } N N \Rightarrow \text{dog food } N \Rightarrow \text{dog food can}$
- We can represent this as an automaton, with a *stack* at each state:



- Generally cannot be represented with finite-state automaton

Parse Tree, Derivation



leftmost derivation

- $S \rightarrow NP VP$
- $NP \rightarrow PRP$
- $PRP \rightarrow \text{we}$
- $VP \rightarrow VBD NP VP$
- $VBD \rightarrow \text{helped}$
- $NP \rightarrow PRP$
- $PRP \rightarrow \text{her}$
- $VP \rightarrow VB NP$
- $VB \rightarrow \text{paint}$
- $NP \rightarrow DT NN$
- $DT \rightarrow \text{the}$
- $NN \rightarrow \text{house}$

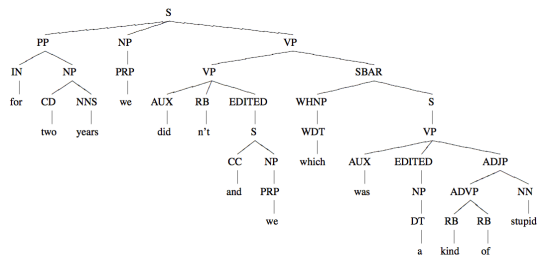
Labeled Bracketing

- Another representation of the same tree:

(S (NP (PRP we)) (VP (VBD helped) (NP (PRP her)) (VP (VB paint) (NP (DT the) (NN house))))))

- Some terminology (review):
 - Terminals are words.
 - Penn Treebank non-terminal set has 2 disjoint subsets:
 - Pre-terminal (POS) tags rewrite to exactly 1 word.
 - The rest never have terminals as children.

Parse Tree, of speech



from Switchboard Corpus

Probabilistic CFGs (PCFGs)

- A PCFG is a CFG with a probability assigned to each rule:

$$P(S \rightarrow NP VP) = P(\text{rhs} = (NP VP) \mid \text{lhs} = S) = P(NP VP \mid S)$$

- Joint probability of the right-hand side (RHS) can be decomposed using the chain rule:

$$P(S \rightarrow NP VP) = P(NP \mid S) * P(VP \mid S, NP) * P(</> \mid S, NP VP)$$

where $</>$ is an "end-of-rule" symbol

- Standard PCFG induction approach
 - Count the number of times rules (local trees) occur
 - Use relative frequency estimation for conditional probabilities

CFG Equivalence

- Two CFGs G and G' are *strongly* equivalent if they describe the same language, and they produce identical trees for strings, modulo node labels
- Two CFGs G and G' are *weakly* equivalent if they describe the same language
- Sometimes a grammar G can be transformed to a weakly equivalent grammar G' that has some beneficial computational properties

Normal Forms

- Chomsky Normal Form (CNF)
 - A grammar $G = (V, T, P, S^1)$ is in CNF if all productions in P are in one of two forms:
 - $A \rightarrow BC$ where $A, B, C \in V$ or
 - $A \rightarrow a$ where $A \in V$ and $a \in T$
- Greibach Normal Form (GNF)
 - A grammar $G = (V, T, P, S^1)$ is in GNF if all productions in P are of the following form:
 - $A \rightarrow aX$ where $A \in V, a \in T$ and $X \in V^*$
- Every CFG G has weakly equivalent CFGs in CNF or GNF
 - Chomsky Normal Form very useful for [chart parsing](#)

Grammar Factorization

- Take a rule from the grammar such as $NP \rightarrow DT JJ NN NNS$ and factor it into multiple rules
- Left factorization:
 - $NP \rightarrow DT NP-DT$
 - $NP-DT \rightarrow JJ NP-DT, JJ$
 - $NP-DT, JJ \rightarrow NN NNS$
- Right factorization:
 - $NP \rightarrow DT-JJ-NN NNS$
 - $DT-JJ-NN \rightarrow DT-JJ NN$
 - $DT-JJ \rightarrow DT JJ$

Penn Treebank CNF

- Disjoint pre-terminal set, so all POS \rightarrow word productions already in CNF
 - Left or right factorization removes productions with > 2 RHS categories
 - Remaining issues:
 - Remove empty categories (0 categories on RHS)
 - Collapse unary productions (1 non-terminal on RHS)
 - remove production $A \rightarrow B$ then do the following:
- | | |
|--------------------------------|------------------------------|
| <u>Productions of the form</u> | <u>Create new production</u> |
| $C \rightarrow X A$ | $C \rightarrow X A B$ |
| $C \rightarrow A X$ | $C \rightarrow A B X$ |
| $C \rightarrow A A$ | $C \rightarrow A B A B$ |
| $B \rightarrow \alpha$ | $A B \rightarrow \alpha$ |

PCFG Induction and Factorization

- Original CFG rules:

$$\hat{P}(A \rightarrow \alpha) = \frac{C(A \rightarrow \alpha)}{\sum_{A \rightarrow \beta \in P} C(A \rightarrow \beta)}$$

- Left factorization:

$$\hat{P}(A \rightarrow B A-B) = \frac{\sum_{\substack{A \rightarrow B\alpha \in P \\ \alpha \in V^k \ k > 1}} C(A \rightarrow B\alpha)}{\sum_{A \rightarrow \beta \in P} C(A \rightarrow \beta)}$$

$$\hat{P}(A-X \rightarrow B A-X-B) = \frac{\sum_{\substack{A \rightarrow XB\alpha \in P \\ \alpha \in V^k \ k > 1}} C(A \rightarrow XB\alpha)}{\sum_{A \rightarrow X\beta \in P} C(A \rightarrow X\beta)}$$

$$\hat{P}(A-X \rightarrow B D) = \frac{C(A \rightarrow X B D)}{\sum_{A \rightarrow X\beta \in P} C(A \rightarrow X\beta)}$$

PCFG Induction and Factorization

- Right factorization

$$\hat{P}(A \rightarrow X_1 \dots X_k B) = \hat{P}(A \rightarrow X_1 \dots X_k B)$$

$$\hat{P}(X_1 \dots X_k \rightarrow X_1 \dots X_{k-1} X_k) = 1$$

- Collapsed unary productions

$$\hat{P}(C \rightarrow X A|B) = \hat{P}(C \rightarrow X A) * \hat{P}(A \rightarrow B)$$

$$\hat{P}(C \rightarrow A|B X) = \hat{P}(C \rightarrow A X) * \hat{P}(A \rightarrow B)$$

$$\hat{P}(A|B \rightarrow \alpha) = \hat{P}(A \rightarrow B) * \hat{P}(B \rightarrow \alpha)$$

Sparsity

- We may observe in our corpus the following rule: $NP \rightarrow DT JJ JJ NN NN NNS$
- We may not observe: $NP \rightarrow DT JJ JJ JJ NN NN NNS$
- Does this mean that the second rule should have zero probability?
- A "Markov" grammar is a factored grammar that provides probability mass to unobserved rules

Left Factorization & “Markov” Grammars

- Take a rule from the grammar such as
NP → DT JJ NN NNS
- Left factorization:
 - NP → DT NP-DT
 - NP-DT → JJ NP-DT, JJ
 - NP-DT, JJ → NN NNS
- Markov grammar, order 1:
 - NP → DT NP-DT
 - NP-DT → JJ NP-JJ “forget” that we saw a DT
 - NP-JJ → NN NP-NN
 - NP-NN → NN

Agenda: Summary

- Questions, comments, concerns?
- Context-Free Grammars
 - Treebanks
 - Inducing CFGs from trees
 - Probabilistic CFGs
- Next week: parsing algorithms