

# Computational Linguistics 1

CMSC/LING 723, LBSC 744



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Lecture 17: 1 November 2011

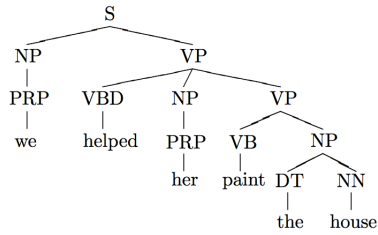
## Agenda

- HW4, due Thursday
- Questions, comments, concerns?
- Parsing algorithms
  - Left-corner grammar transformation
  - Earley parsing
- Context-sensitive grammar formalisms?

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## Parse Tree, Derivation



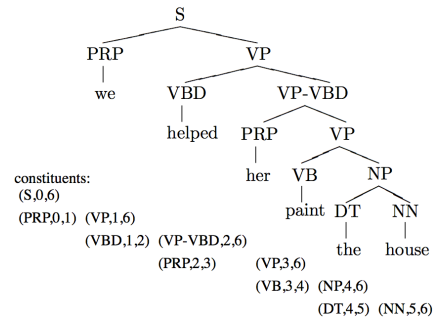
*leftmost derivation*

- S → NP VP
- NP → PRP
- PRP → we
- VP → VBD NP VP
- VBD → helped
- NP → PRP
- PRP → her
- VP → VB NP
- VB → paint
- NP → DT NN
- DT → the
- NN → house

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## Parse Tree, CNF



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## CYK Chart, span 4, midpoint 3

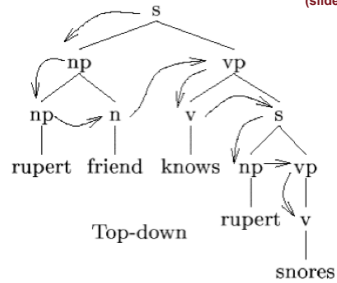
Span			
4	(NP, 0.015, 1, NN, NP)	(NP, 0.025, 2, NP, NP)	(NP, 0.045, 3, NP, NN)
3	(NP, 0.15, 2, NP, NN)	(NP, 0.15, 3, NP, NN)	
2	(NP, 0.5, 1, NN, NN)	(NP, 0.5, 2, NN, NN)	(NP, 0.5, 3, NN, NN)
1	NN	NN	NN

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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)

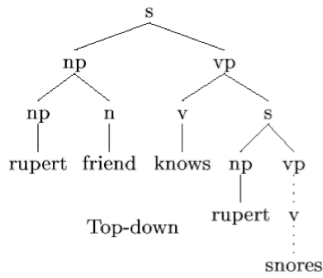


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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)



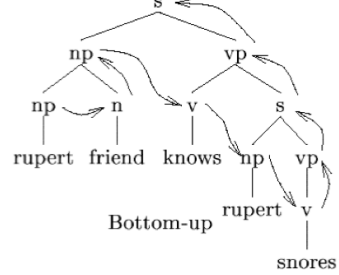
Intuitive?

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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)

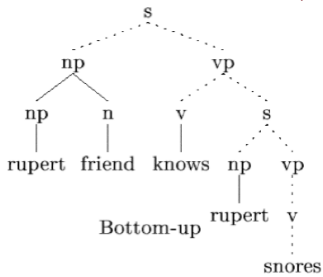


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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)



Intuitive?

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## Left-corner Parsing

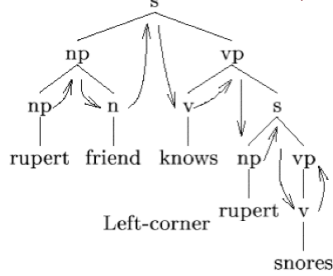
- The left corner of a context-free rule is the first symbol on the right hand side:  
 $S \rightarrow NP VP$ : left corner is NP.
- The left-corner of each production is recognized bottom-up, and everything else is predicted top-down

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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)

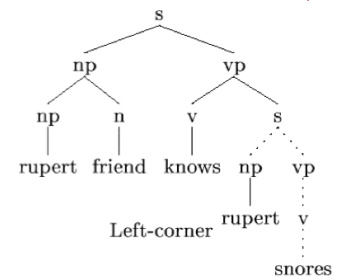


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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)



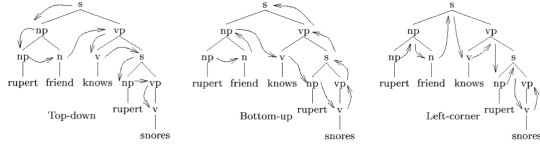
Intuitive?

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## Top-down, Bottom-up, Left-corner

(slide adapted from Mark Johnson)



- **Top-down:**
  - Right-recursive grammars require finite state size
  - But left-recursive grammars require *unbounded* state size
- **Left-corner**
  - Finite-state size for both left-recursive and right-recursive grammars
  - Only center-embedded structures require unbounded stacks
  - ...which emulates human behavior!

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## Top-down, Bottom-up, Left-corner

- **Top-down:**
  - Right-recursive grammars require finite state size
  - But left-recursive grammars require *unbounded* state size
- **Left-corner**
  - Finite-state size for both left-recursive and right-recursive grammars
  - Only center-embedded structures require unbounded stacks
  - ...which emulates human behavior!

From [Resnik, 1992]:

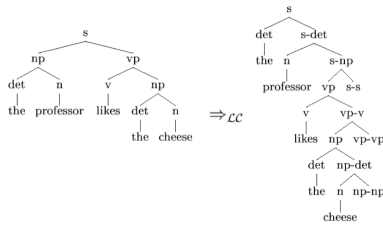
Strategy	Space required		
	Left	Center	Right
Top-down	$O(n)$	$O(n)$	$O(1)$
Bottom-up	$O(1)$	$O(n)$	$O(n)$
Left-corner <sup>†</sup>	$O(1)$	$O(n)$	$O(1)$
<b>What people do</b>	$O(1)$	$O(n)$	$O(1)$

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## Building a Left-corner Parser?

- Perform a left-corner transform on grammar  $G$ , then can use a top-down parser
  - because the LC-transform converts left-recursion into right-recursion



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## Left-corner Grammar Transform

- $A \rightarrow aAa$  for all  $A \in V, a \in T$
- $A \rightarrow A-C$  for all  $A \in V, C \rightarrow \epsilon \in P$
- $A-X \rightarrow \beta A-B$  for all  $A \in V, B \rightarrow X\beta \in P$
- $A-A \rightarrow \epsilon$  for all  $A \in V$

- After transforming the grammar, do ... what?

**CYK!**

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## Agenda

- HW4, due Thursday
- Parsing algorithms
  - Left-corner grammar transform
  - Earley parsing
- Context-sensitive grammar formalisms

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## CKY: Analysis

- Since it's bottom up, CKY populates the table with a lot of "phantom constituents"
  - Spans that are constituents, but cannot really occur in the context in which they are suggested
- Conversion of grammar to CNF adds additional non-terminal nodes
  - Leads to weak equivalence wrt original grammar
  - Additional terminal nodes not (linguistically) meaningful: but can be cleaned up with post processing
- Is there a parsing algorithm for arbitrary CFGs that combines dynamic programming and top-down control?

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## Earley Parsing Algorithm

- One advantage of top-down over bottom-up is that one never builds constituents that cannot be rooted
- Earley parsing motivation
  - Only want to build categories that can be rooted
  - Use a top-down *filter*
  - Use a chart parsing approach
- Dynamic programming algorithm (surprise)
- Allows arbitrary CFGs
- Fills a chart in a single sweep over the input

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## Earley Parsing: Chart, States

- Chart is an array of length  $N + 1$ , where  $N$  = number of words
- Chart entries represent states:
  - Completed constituents and their locations
  - In-progress constituents
  - Predicted constituents
- Each state contains three items of information:
  - A grammar rule
  - Information about progress made in completing the sub-tree represented by the rule
  - Span of the sub-tree

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## Chart Entries: State Examples

- $S \rightarrow \bullet VP [0,0]$ 
  - A VP is predicted at the start of the sentence
- $NP \rightarrow Det \bullet Nominal [1,2]$ 
  - An NP is in progress; the Det goes from 1 to 2
- $VP \rightarrow V NP \bullet [0,3]$ 
  - A VP has been found starting at 0 and ending at 3

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## Earley in a nutshell

- Start by predicting S
- Step through chart:
  - New predicted states are created from current states
  - New incomplete states are created by advancing existing states as new constituents are discovered
  - States are completed when rules are satisfied
- Termination: look for  $S \rightarrow \alpha \bullet [0, N]$

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## Earley Algorithm

```
function EARLEY-PARSE(words, grammar) returns chart
  ENQUEUE( $\gamma \rightarrow \bullet S, [0,0], chart[0]$ )
  for  $i$  ← from 0 to LENGTH(words) do
    for each state in chart[i] do
      if INCOMPLETE?(state) and
        NEXT-CAT(state) is not a part of speech then
        PREDICTOR(state)
      elseif INCOMPLETE?(state) and
        NEXT-CAT(state) is a part of speech then
        SCANNER(state)
      else
        COMPLETER(state)
    end
  end
  return(chart)
```

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## Earley Algorithm

```
procedure PREDICTOR( $A \rightarrow \alpha \bullet B \beta, [i, j]$ )
  for each ( $B \rightarrow \gamma$ ) in GRAMMAR-RULES-FOR( $B, grammar$ ) do
    ENQUEUE( $B \rightarrow \bullet \gamma, [j, j], chart[j]$ )
  end
procedure SCANNER( $A \rightarrow \alpha \bullet B \beta, [i, j]$ )
  if  $B \subset$  PARTS-OF-SPEECH(word[j]) then
    ENQUEUE( $B \rightarrow word[j], [j, j+1], chart[j+1]$ )
  end
procedure COMPLETER( $B \rightarrow \gamma \bullet, [j, k]$ )
  for each ( $A \rightarrow \alpha \bullet B \beta, [i, j]$ ) in chart[j] do
    ENQUEUE( $A \rightarrow \alpha B \bullet \beta, [i, k], chart[k]$ )
  end
```

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## Earley Example

- Input: Book that flight
- Desired end state:  $S \rightarrow \alpha \cdot [0,3]$ 
  - Meaning: S spanning from 0 to 3, completed rule

## Earley: Chart[0]

S0	$\gamma \rightarrow \bullet S$	[0,0]	Dummy start state
S1	$S \rightarrow \bullet NP VP$	[0,0]	Predictor
S2	$S \rightarrow \bullet Aux NP VP$	[0,0]	Predictor
S3	$S \rightarrow \bullet VP$	[0,0]	Predictor
S4	$NP \rightarrow \bullet Pronoun$	[0,0]	Predictor
S5	$NP \rightarrow \bullet Proper-Noun$	[0,0]	Predictor
S6	$NP \rightarrow \bullet Det Nominal$	[0,0]	Predictor
S7	$VP \rightarrow \bullet Verb$	[0,0]	Predictor
S8	$VP \rightarrow \bullet Verb NP$	[0,0]	Predictor
S9	$VP \rightarrow \bullet Verb NP PP$	[0,0]	Predictor
S10	$VP \rightarrow \bullet Verb PP$	[0,0]	Predictor
S11	$VP \rightarrow \bullet VP PP$	[0,0]	Predictor

Note that given a grammar, these entries are the same for all inputs; they can be pre-loaded...

## Earley: Chart[1]

S12	$Verb \rightarrow book \bullet$	[0,1]	Scanner
S13	$VP \rightarrow Verb \bullet$	[0,1]	Completer
S14	$VP \rightarrow Verb \bullet NP$	[0,1]	Completer
S15	$VP \rightarrow Verb \bullet NP PP$	[0,1]	Completer
S16	$VP \rightarrow Verb \bullet PP$	[0,1]	Completer
S17	$S \rightarrow VP \bullet$	[0,1]	Completer
S18	$VP \rightarrow VP \bullet PP$	[0,1]	Completer
S19	$NP \rightarrow \bullet Pronoun$	[1,1]	Predictor
S20	$NP \rightarrow \bullet Proper-Noun$	[1,1]	Predictor
S21	$NP \rightarrow \bullet Det Nominal$	[1,1]	Predictor
S22	$PP \rightarrow \bullet Prep NP$	[1,1]	Predictor

## Earley: Chart[2] and Chart[3]

S23	$Det \rightarrow that \bullet$	[1,2]	Scanner
S24	$NP \rightarrow Det \bullet Nominal$	[1,2]	Completer
S25	$Nominal \rightarrow \bullet Noun$	[2,2]	Predictor
S26	$Nominal \rightarrow \bullet Nominal Noun$	[2,2]	Predictor
S27	$Nominal \rightarrow \bullet Nominal PP$	[2,2]	Predictor
S28	$Noun \rightarrow flight \bullet$	[2,3]	Scanner
S29	$Nominal \rightarrow Noun \bullet$	[2,3]	Completer
S30	$NP \rightarrow Det Nominal \bullet$	[1,3]	Completer
S31	$Nominal \rightarrow Nominal \bullet Noun$	[2,3]	Completer
S32	$Nominal \rightarrow Nominal \bullet PP$	[2,3]	Completer
S33	$VP \rightarrow Verb NP \bullet$	[0,3]	Completer
S34	$VP \rightarrow Verb NP \bullet PP$	[0,3]	Completer
S35	$PP \rightarrow \bullet Prep NP$	[3,3]	Predictor
S36	$S \rightarrow VP \bullet$	[0,3]	Completer
S37	$VP \rightarrow VP \bullet PP$	[0,3]	Completer

## Earley: Recovering the Parse

As with CKY, add backpointers...

Chart[1]	S12	$Verb \rightarrow book \bullet$	[0,1]	Scanner
Chart[2]	S23	$Det \rightarrow that \bullet$	[1,2]	Scanner
Chart[3]	S28	$Noun \rightarrow flight \bullet$	[2,3]	Scanner
	S29	$Nominal \rightarrow Noun \bullet$	[2,3]	(S28)
	S30	$NP \rightarrow Det Nominal \bullet$	[1,3]	(S23, S29)
	S33	$VP \rightarrow Verb NP \bullet$	[0,3]	(S12, S30)
	S36	$S \rightarrow VP \bullet$	[0,3]	(S33)

## Earley: Efficiency

- For such a simple example, there seems to be a lot of useless stuff...
- Why?

## Back to Ambiguity

- Did we solve it?
- No: both CKY and Earley return multiple parse trees...
  - Plus: compact encoding with shared sub-trees
  - Plus: work deriving shared sub-trees is reused
  - Minus: neither algorithm tells us which parse is correct

## Ambiguity

- Why don't humans usually encounter ambiguity?
- How can we improve our models?

## Agenda: Summary

- HW4, due Thursday
- Parsing algorithms
  - Earley parsing
  - Left-corner grammar transform
- Next time: context-sensitive grammar formalisms