# Computational Linguistics 1 CMSC/LING 723, LBSC 744



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Agenda

- Readings
- HW1 due next Tuesday
- Questions?
- Language Models Smoothing
- Evaluating LMs

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Morphemes to Orthographic Form ^: ε othe q\_ q, #. other FOX S# Computational Linguistics 1





# Agenda

- Readings
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- Questions?

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- Language Models
- Smoothing
- Evaluating LMs

#### N-Gram Language Models

What?

- Language Models assign probabilities to sequences of tokens
- Why?
- Statistical machine translation
- Speech recognition
- Handwriting recognition
- Predictive text input
- How?

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- Based on previous word histories
- n-gram = consecutive sequences of tokens

DescriptionDescriptionThis is a sentenceUnigrams:<br/>This,<br/>is,<br/>a,<br/>sentence

# N-Gram Language Models N=2 (bigrams) This (s) sentence Bigrams: This is, is a, a sentence Sentence of length s, how many bigrams?



## **Computing Probabilities**

 $P(w_1, w_2, \ldots, w_T)$ 

 $= P(w_1)P(w_2|w_1)P(w_3|w_1,w_2)\dots P(w_T|w_1,\dots,w_{T-1})$  [chain rule]

#### Is this practical?

No! Can't keep track of all possible histories of all words!

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## **Approximating Probabilities**

**Basic idea:** limit history to fixed number of words N (Markov Assumption)

 $P(w_k|w_1,...,w_{k-1}) \approx P(w_k|w_{k-N+1},...,w_{k-1})$ 

#### N=I: Unigram Language Model

 $P(w_k|w_1,\ldots,w_{k-1}) \approx P(w_k)$ 

 $\Rightarrow P(w_1, w_2, \dots, w_T) \approx P(w_1)P(w_2) \dots P(w_T)$ 

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#### **Approximating Probabilities**

**Basic idea:** limit history to fixed number of words N (Markov Assumption)

 $P(w_k|w_1,...,w_{k-1}) \approx P(w_k|w_{k-N+1},...,w_{k-1})$ 

#### N=2: Bigram Language Model

 $P(w_k|w_1,\ldots,w_{k-1}) \approx P(w_k|w_{k-1})$ 

 $\Rightarrow P(w_1, w_2, \dots, w_T) \approx P(w_1 | < \mathbf{S} >) P(w_2 | w_1) \dots P(w_T | w_{T-1})$ 

#### Approximating Probabilities

**Basic idea:** limit history to fixed number of words N (Markov Assumption)

 $P(w_k|w_1,...,w_{k-1}) \approx P(w_k|w_{k-N+1},...,w_{k-1})$ 

#### N=3: Trigram Language Model

 $P(w_k|w_1,\ldots,w_{k-1}) \approx P(w_k|w_{k-2},w_{k-1})$ 

 $\Rightarrow P(w_1, w_2, \dots, w_T) \approx P(w_1 | < \mathbf{S} > < \mathbf{S} >) \dots P(w_T | w_{T-2} w_{T-1})$ 

# Building N-Gram Language Models

- Use existing sentences to compute n-gram probability estimates (training)
- Terminology:

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- N = total number of words in training data (tokens)
- V = vocabulary size or number of unique words (types)
- + C( $w_1,...,w_k$ ) = frequency of n-gram  $w_1, ..., w_k$  in training data
- + P( $w_1, ..., w_k$ ) = probability estimate for n-gram  $w_1 ... w_k$
- $\mathsf{P}(w_k|w_1,\,...,\,w_{k-1})$  = conditional probability of producing  $w_k$  given the history  $w_1,\,...,\,w_{k-1}$

## **Building N-Gram Models**

- · Start with what's easiest!
- Compute maximum likelihood estimates for individual n-gram probabilities

• Unigram: 
$$P(w_i) = \frac{C(w_i)}{N}$$

• Bigram:  $P(w_i, w_j) = \frac{C(w_i, w_j)}{N}$ 

$$P(w_j|w_i) = \frac{P(w_i, w_j)}{P(w_i)} = \frac{C(w_i, w_j)}{\sum C(w_i, w_j)} = \frac{C(w_i, w_j)}{C(w_i)}$$

- · Uses relative frequencies as estimates
- Maximizes the likelihood of the data given the model  $\mathsf{P}(\mathsf{D}|\mathsf{M})$

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## Data Sparsity

- · Serious problem in language modeling!
- Increase N?
  - Larger N = more context
  - Lexical co-occurrences Local syntactic relations
- More context is better?Larger N = more complex model
- For example, assume a vocabulary of 100,000
- How many parameters for unigram LM? Bigram? Trigram?
- · Data sparsity becomes even more severe as N increases
- Solution 1: Use larger training corpora
- · Can't always work ... Blame Zipf's Law (Looong tail)
- Solution 2: Assign non-zero probability to unseen n-grams · Known as smoothing

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## Agenda

- Language Models
- Smoothing

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Evaluating LMs

#### Smoothing

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- Zeros are bad for any statistical estimator
- · Need better estimators because MLEs give us a lot of zeros
- · A distribution without zeros is "smoother"
- The Robin Hood Philosophy: Take from the rich (seen ngrams) and give to the poor (unseen n-grams)
- And thus also called discounting
- Critical: make sure you still have a valid probability distribution!
- · Language modeling: theory vs. practice

## Laplace's Law

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- · Simplest and oldest smoothing technique
- · Just add 1 to all n-gram counts including the unseen ones
- · So, what do the revised estimates look like?

Laplace's Law: Probabilities  $P_{MLE}(w_i) = \frac{C(w_i)}{N} \qquad \longrightarrow \qquad P_{LAP}(w_i) = \frac{C(w_i) + 1}{N + V}$ 
$$\begin{split} P_{MLE}(w_i,w_j) &= \frac{C(w_i,w_j)}{N} \longrightarrow P_{LAP}(w_i,w_j) = \frac{C(w_i,w_j)+1}{N+V^2} \\ \text{Careful, don't confuse the N's!} \\ P_{LAP}(w_j|w_i) &= \frac{P_{LAP}(w_i,w_j)}{P_{LAP}(w_i)} = \frac{C(w_i,w_j)+1}{C(w_i)+V} \end{split}$$
What if we don't know V? Computational Linguistics 1

# Laplace's Law · Bayesian estimator with uniform priors Moves too much mass over to unseen n-grams · What if we added a fraction of 1 instead?

#### Lidstone's Law of Succession

- Add 0 <  $\gamma$  < 1 to each count instead
- The smaller  $\gamma$  is, the lower the mass moved to the unseen n-grams (0=no smoothing)
- The case of  $\gamma$  = 0.5 is known as Jeffery-Perks Law or Expected Likelihood Estimation
- How to find the right value of y?

#### Good-Turing Estimator

- Intuition: Use n-grams seen once to estimate n-grams never seen and so on
- Compute  $N_r$  (frequency of frequency r)  $N_r = \sum 1$

$$w_i w_j : C(w_i w_j)$$

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- $N_0$  is the number of items with count 0
- *N*<sub>1</sub> is the number of items with count 1
  ...

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**Good-Turing Estimator** • For each *r*, compute an expected frequency estimate smoothed count:  $r' = C_{GT}(w_i, w_j) = (r+1)\frac{N_{r+1}}{N_r}$ • Replace MLE counts of seen bigrams with the expected frequency estimates and use those for probabilities  $P_{GT}(w_i, w_j) = \frac{C_{GT}(w_i, w_j)}{N} \qquad P_{GT}(w_j | w_i) = \frac{C_{GT}(w_i, w_j)}{C(w_i)}$ 







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## Good-Turing Estimator

- Can't replace all MLE counts
- What about r<sub>max</sub>?

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- $N_{r+1} = 0$  for  $r = r_{max}$
- Solution 1: Only replace counts for r < k (~10)
- Solution 2: Fit a curve S through the observed (r,  $N_r$ ) values and use S(r) instead
- For both solutions, remember to do what?
- Bottom line: the Good-Turing estimator is not used by itself but in combination with other techniques

# Agenda

- Language Models
  Smoothing
- Combining estimators
- Evaluating LMs

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## Agenda: Summary

- Language Models
- · Assign probabilities to sequences of tokens
- N-gram language models
- Consider only limited histories
- Data sparsity
- · Smoothing to the rescue!
- Variations on a theme: different techniques for redistributing probability mass
- Important: make sure you still have a valid probability distribution!
- Evaluating LMs

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# Combining Estimators

- Better models come from:
- $\boldsymbol{\cdot}$  Combining n-gram probability estimates from different models
- Leveraging different sources of information for prediction
- Three major combination techniques:
- Simple Linear Interpolation of MLEs
- Katz Backoff
- Kneser-Ney Smoothing

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## Linear MLE Interpolation

Mix a trigram model with bigram and unigram models to offset sparsity

Mix = Weighted Linear Combination

#### $P(w_k|w_{k-2}w_{k-1}) =$

 $\lambda_1 P(w_k | w_{k-2} w_{k-1}) + \lambda_2 P(w_k | w_{k-1}) + \lambda_3 P(w_k)$ 

$$0 <= \lambda_i <= 1 \qquad \sum_i \lambda_i = 1$$

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# Linear MLE Interpolation *λ<sub>i</sub>* are estimated on some held-out data set (not training, not test) Estimation is usually done via an EM variant or other numerical algorithms (e.g. Powell)



#### **Backoff Models**

- Consult different models in order depending on specificity (instead of all at the same time)
- The most detailed model for current context first and, if that doesn't work, back off to a lower model
- Continue backing off until you reach a model that has some counts

#### **Backoff Models**

- Important: need to incorporate discounting as an integral part of the algorithm... Why?
- MLE estimates are well-formed...
- But, if we back off to a lower order model without taking something from the higher order MLEs, we are adding extra mass!
- Katz backoff

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- Starting point: GT estimator assumes uniform distribution over unseen events... can we do better?
- Use lower order models!

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**Katz Backoff Given a trigram "x y z"**  $P_{katz}(z|x, y) = \begin{cases} P_{GT}(z|x, y), & \text{if } C(x, y, z) > 0\\ \alpha(x, y)P_{katz}(z|y), & \text{otherwise} \end{cases}$   $P_{katz}(z|y) = \begin{cases} P_{GT}(z|y), & \text{if } C(y, z) > 0\\ \alpha(y)P_{GT}(z), & \text{otherwise} \end{cases}$ Computational Linguistics 1

# Katz Backoff Why use P<sub>GT</sub> and not P<sub>MLE</sub> directly ? If we use P<sub>MLE</sub> then we are adding extra probability mass when backing off! Another way: Can't save any probability mass for lower order models without discounting Why the α's? To ensure that total mass from all lower order models sums exactly to what we got from the discounting

#### **Kneser-Ney Smoothing**

- Observation:
- Average Good-Turing discount for r ≥ 3 is largely constant over r
   So, why not simply subtract a fixed discount D (≤1) from non-zero counts?
- Absolute Discounting: discounted bigram model, back off to MLE unigram model
- Kneser-Ney: Interpolate discounted model with a special "continuation" unigram model

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#### **Kneser-Ney Smoothing**

#### Intuition

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- Lower order model important only when higher order model is sparse
- Should be optimized to perform in such situations

#### Example

- C(Los Angeles) = C(Angeles) = M; M is very large
- "Angeles" always and only occurs after "Los"
- Unigram MLE for "Angeles" will be high and a normal backoff algorithm will likely pick it in any context
- It shouldn't, because "Angeles" occurs with only a single context in the entire training data

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# Explicitly Modeling OOV

- Fix vocabulary at some reasonable number of wordsDuring training:
  - During training:
- Consider any words that don't occur in this list as unknown or out of vocabulary (OOV) words
- Replace all OOVs with the special word <UNK>
- Treat <UNK> as any other word and count and estimate probabilities
- · During testing:

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- Replace unknown words with <UNK> and use LM
- · Test set characterized by OOV rate (percentage of OOVs)

Agenda: Summary

- Language Models
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• Evaluating LMs: Perplexity

# Most common: Perplexity assigned by the trained LM to a test set

- Perplexity: How surprised are you on average by what comes next ?
- If the LM is good at knowing what comes next in a sentence ⇒ Low perplexity (lower is better)
- Relation to weighted average branching factor

**Evaluating Language Models** 

Information theoretic criteria used

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## Computing Perplexity

- Given testset W with words  $w_1, ..., w_N$
- Treat entire test set as one word sequence
- Perplexity is defined as the probability of the entire test set normalized by the number of words  $PP(T)=P(w_1,\ldots,w_N)^{-1/N}$
- Using the probability chain rule and (say) a bigram LM, we can write this as

$$PP(T) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

A lot easer to do with log probs!

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#### **Practical Evaluation** Use <s> and </s> both in probability computation • Count </s> but not <s> in N Typical range of perplexities on English text is 50-1000 · Closed vocabulary testing yields much lower perplexities Testing across genres yields higher perplexities Can only compare perplexities if the LMs use the same vocabulary Trigram Order Unigram Bigram PP 962 170 109 Training: N=38 million, V~20000, open vocabulary, Katz backoff where applicable Test: 1.5 million words, same genre as training

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## Typical "State of the Art" LMs

- Training
  N = 10 billion words, V = 300k words
  - 4-gram model with Kneser-Ney smoothing
- Testing
- 25 million words, OOV rate 3.8%
- Perplexity ~50

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- Data sparsity Smoothing to the rescue!
- · Variations on a theme: different techniques for redistributing
- probability mass
- Important: make sure you still have a valid probability distribution!
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